

**MATH10282: INTRODUCTION TO STATISTICS**  
**SEMESTER 2**  
**QUIZ PROBLEM 2**  
(Deadline: Thursday 25 February 2021, 10:00am)

Suppose that  $X_1, \dots, X_n$  is a random sample from a distribution specified by the probability density function

$$f_X(x) = ax^{a-1}$$

for  $a > 0$  and  $0 < x < 1$ . What are the mean and variance of the sampling distribution of the sample mean,  $\bar{X}$ ?

- a) mean =  $\frac{a}{a+1}$ , variance =  $\frac{a}{(a+2)(a+1)^2}$ .
- b) mean =  $\frac{a}{a+1}$ , variance =  $\frac{a}{n(a+2)(a+1)}$ .
- c) mean =  $\frac{a}{a+1}$ , variance =  $\frac{a}{n(a+2)(a+1)^2}$ .
- d) mean =  $\frac{a}{a+1}$ , variance =  $\frac{a}{n(a+1)^2}$ .

**This problem is worth 1 mark. Marking scheme: 1 mark if the answer is correct, 0 mark if the answer is incorrect.**

**Please use Blackboard to enter your answer.**