

MATH10282: INTRODUCTION TO STATISTICS
SEMESTER 2
QUIZ PROBLEM 3
(Deadline: Tuesday 18 February 2020, 9:00am)

Let $x_1, x_2, \dots, x_n$ denote a data set and let $x_{(1)} \leq x_{(2)} \leq \dots \leq x_{(n)}$ denote the order statistics in ascending order. Show that

$$\text{sample first quartile} = \begin{cases} x_{(m)} + \frac{1}{4} [x_{(m+1)} - x_{(m)}], & \text{if } n = 4m, \\ x_{(m)}, & \text{if } n = 4m - 1, \\ x_{(m-1)} + \frac{3}{4} [x_{(m)} - x_{(m-1)}], & \text{if } n = 4m - 2, \\ x_{(m-1)} + \frac{1}{2} [x_{(m)} - x_{(m-1)}], & \text{if } n = 4m - 3, \end{cases}$$

where m is an integer greater than or equal to 1.

This problem is worth 1 mark. Marking scheme: 1 mark if the answer is correct, and the derivation is correct and detailed enough; 0.5 mark if the answer is correct, and the derivation is incorrect or not detailed enough; 0.5 mark if the answer is incorrect or not given, but the derivation is correct and detailed enough; 0 mark if the answer is correct, but the derivation is not detailed enough; 0 mark if the answer is incorrect, and the derivation is not detailed enough.

You can give your written solution to me during any of the lectures or example classes. You can also bring your solution to ATB2.223, place it under the door if I am not in. Email submissions or late submissions will not be accepted. I will mark your solutions and email your mark and your scanned working to you within 24 hours of the deadline. **PLEASE DO NOT FORGET TO WRITE YOUR FULL NAME AND ID.**