

MATH4/68181: Extreme values and financial risk
Semester 1
Problem sheet 9

Suppose stock returns of a company follow an exponential distribution with random parameter λ . Determine the actual distribution of stock returns if λ follows the

1. exponential distribution with parameter a , a is an unknown parameter,
2. uniform $[a, b]$ distribution, both a and b are unknown parameters,
3. power function distribution with pdf $a\lambda^{a-1}$, $0 < \lambda < 1$, a is an unknown parameter,
4. Pareto distribution with pdf aK^a/λ^{a+1} , $\lambda > K$, both a and K are unknown parameters.

In each case, estimate the unknown parameters by the method of maximum likelihood.